EXPLORING THE DEPENDENCE OF GALAXY PROPERTIES ON GROUP HALO ENVIRONMENT IN THE ECO CATALOG

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ABSTRACT

We discuss the development of an optimized halo mass metric based on galaxy group dynamics as well as its application to understanding the dependence of galaxy properties on environment at low redshift. Methods and parameters for group finding and calculating dynamical mass are optimized on a mock catalog with similar redshift range and magnitude limit to the RESOLVE survey, a mass census of > 50,000 cubic Mpc of the nearby cosmic web (cz = 4500 - 7000 km/sec, $M_r \lesssim -17$). Optimal friends-of-friends linking lengths for dynamical mass measurements are determined to be 0.12 and 1.3 for $b_1$ and $b_2$, respectively. We also apply tests for characterizing the virialization state of a group including the Anderson-Darling test and the Dressler-Schechtman test for identifying substructure. These methods are applied to a sample of galaxies in the ECO catalog, a 10x larger volume-limited survey that encloses the A-semester volume of RESOLVE. Using both halo mass and halo evolutionary state to quantify environment, we study environmental influences on galaxy properties such as color, gas content, and star formation history. We find that over 80% of field galaxies reside on the blue sequence, while galaxies within the virial radius of groups with halo mass greater than $10^{13.5} M_\odot$ uniformly contain the lowest fraction of blue-sequence galaxies. Above this same mass scale groups uniformly have recent histories of very little star formation. This halo mass scale may correspond to an evolutionary transition in galaxy groups after which processes such as quenching become substantially more effective or permanent.

Keywords: galaxies: clusters — galaxies: evolution

1. INTRODUCTION

The Universe as we observe it today is full of large-scale structure populated by galaxies often residing in gravitationally bound groups or clusters. These massive systems are contained within dark matter halos that contribute to forming very dense environments as indicated by the large velocities of observed group member galaxies. Differences between the properties of galaxies in these high mass groups and isolated galaxies presumably living in less dense environments led to the hypothesis of various evolutionary scenarios. For example, mechanical processes such as ram pressure or viscous stripping of cold gas (Gunn & Gott 1972; Nulsen 1982; Quilis et al. 2000), galaxy mergers & interactions (Holmberg 1941; Bekki 1998), and ‘strangulation’ that causes the loss of a fresh gas supply due to the stripping of warm and hot gas as galaxies fall into the potential well of their cluster (Balogh et al. 2000; Larson et al. 1980; Rasmussen et al. 2008; Kawata & Mulchaey 2008) can all explain the connections between environment and observed galaxy properties such as star formation rate (Weinmann et al. 2006; Zabludoff & Mulchaey 1998), color (Tanaka & Kodama 2004), galaxy morphology (Dressler et al. 1997), and HI content (Giovanelli & Haynes 1985; Kawata & Mulchaey 2008). These studies repeatedly show evidence in support of processes that would create the ‘red and dead’ galaxies observed in dense group environments (Cohen et al. 2014; Wetzel et al. 2013; Weinmann et al. 2011; Li 2007). Studies also have investigated differences in galaxies based on whether or not they are in a virialized state (Carollo et al. 2013; Hou et al. 2009). While there is much evidence for a difference between the properties of group and field galaxies, it is still unclear at what mass scales they take place and to what radius these processes still have an effect (Bahé et al. 2013). It is also still uncertain which processes dominate a galaxy’s transition to becoming red and dead as commonly observed in dense halo environments (Wetzel et al. 2012). It is therefore important to study the properties of groups’ satellite galaxies at all radii for a complete variety of host halo masses.

In order to study galaxy properties as a function of halo environment, accurate group finding and mass estimation of these systems are necessary in order to properly define the environment. There are several methods to determine group mass, including X-ray observations, gravitational lensing, abundance matching, and dynamical mass methods. Using X-ray emission from gas in groups requires robust scaling relations between mass and X-ray luminosity or X-ray temperature (Zhao et al. 2013; Takey et al. 2011). This approach requires substantial observing time and is not ideal for large samples of data or low mass groups. Gravitational lensing is also not ideal since only massive clusters will provide sufficient lensing to distort background objects (Applegate et al. 2014). An advantage of this method though, is that it is independent of group dynamical state (Jauzac et al. 2012; Becker & Kravtsov 2011).

Halo abundance matching (HAM) and dynamical mass determination methods are both easily applied to large samples of galaxies and are therefore used in this paper. HAM assigns halo masses to groups based on the
total luminosity of all the member galaxies by assuming a monotonic relationship between group mass and group luminosity. This mass assignment utilizes an accepted total luminosity distribution and a halo mass function and assigns masses by equating the two at equal abundances. The application of this method is straightforward, only requiring luminosities, positions, and redshifts of galaxies. It is also capable of returning halo masses for all groups, regardless of the number of members. There are negatives to using HAM such as introducing covariance with luminosity in the resulting group masses. HAM also does not utilize group dynamical information in estimating halo masses, which may in some cases be a better representation of a group’s mass. More details on HAM can be found in §3.2 and §4.2.

Group dynamical masses are found using kinematic information that is derived from the positions and velocities of all group members. By applying the virial formula to a galaxy group system, Eq. 1 can be derived, where \( G \) is the gravitational constant, \( \sigma \) is the line-of-sight group velocity dispersion, and \( r_{\text{vir}} \) is the group virial radius (Girardi et al. 1998).

\[
M_{\text{dyn}} = \frac{3\pi \sigma^2 r_{\text{vir}}}{2G} \tag{1}
\]

Applying Eq. 1 to all groups will incorrectly assess the masses of unrelaxed groups (Evrard 1987). Discrepancies due to this are not severe on average, and in fact can be revealing in certain cases when compared to masses found using HAM. This method becomes less reliable for groups with fewer than 5 members because of low number statistics. This mass measurement eliminates covariance with luminosity and other related group properties in contrast to the abundance matching method. For this reason the dynamical mass method is used in this paper, although masses found using abundance matching are used for comparison.

The goal of this paper is to understand and improve the method of determining group dynamical masses, and then to apply these methods to groups in the ECO catalog in order to study the effects of halo environment on selected galaxy group properties. These data are described in §2.1. In §2.2 I discuss the mock catalog used to optimize various methods used later on the real data including group finding (§3.1), halo mass measurements (§3.2), and estimation of virial radius and virial state (§3.3). Results are presented in section 4, starting with the optimization of linking lengths for group finding in §4.1, followed by a comparison of two mass measurements for groups in ECO in §4.2 and the results of testing for substructure in ECO groups in §4.3, and ending with the results of studying the environmental effects on color and star formation in §4.4.

2. DATA

For this study a cosmology with \( H_0 = 70 \text{ km/s/Mpc} \) is assumed. Mock catalog related values were computed in units of \( h \), where \( H_0 = 100h \text{ km/s/Mpc} \), but were converted to match the units of the real data. Simulated data are used to optimize methods for group finding so the most accurate dynamical group masses can be determined for the observed data. The ECO catalog serves as the observed data, which will be later studied to determine environmental effects on galaxy properties. Both the observed and simulated data samples are discussed in this section in detail.

2.1. The ECO Catalog

The sample of galaxies used in this study comes from the ECO, or Environmental COntext, catalog (Moffett et al. submitted) and the REsolved Spectroscopy Of A Local VolumE (RESOLVE) survey (Kannappan et al., in prep). Sky coverage for ECO is shown in Fig. 1 with the RESOLVE-A semester boxed in green and galaxies color coded by their groups’ halo mass. ECO was constructed to provide a large sample to achieve good statistics and offer large-scale environmental context for RESOLVE-A. The sample contains a variety of environments including voids, filaments, groups, and a few large clusters.

The ECO catalog contains 12,864 galaxies in a 603,600 Mpc\(^3\) volume. About 4,270 of these galaxies live in 340 groups that contain greater than 5 members. The sample is complete for \( M_\text{r} < -17.33 \). Redshifts for all member galaxies were obtained from overlapping surveys: the Sloan Digital Sky Survey (SDSS) (York et al. 2000) data, the Updated Zwicky Catalog (UZC, Falco et al. 1999), RESOLVE (Kannappan et al., in prep.), HyperLEDA (Paturel et al. 2003), GAMA (Driver et al. 2011), 2dF (Colless et al. 2001), and 6dF (Jones et al. 2009). The ECO redshift limits are 3000 km/s < \( cz < 7000 \text{ km/s} \), with 470 km/s additional buffers on either end corresponding to about 1 Mpc. Similar buffers exist in RA and DEC coordinates. These buffer regions are used to reduce edge effects by removing galaxy groups whose centers fall outside the edge of these boundaries and also adding in galaxies that lie in fingers of god that poke out of the volume.

Custom photometry was performed to obtain SDSS ugriz, GALEX NUV, and 2MASS JHK magnitudes for ECO galaxies (see Moffett et al., submitted). For each galaxy, these data were used to derive the fractional stellar mass growth rate (FSMGR), which quantifies the ratio of star formation that happened in the last gigayear of a galaxy’s lifetime to all prior star formation, based on stellar population modeling. Unlike a specific star formation rate, this parameter is defined such that it can exceed one (Kannappan et al. 2013).

A subset of ECO galaxies named “ECO+A” overlaps with HI data from the public Arcebi Legacy Fast ALFA \( \alpha \cdot 0.40 \) catalog (Haynes & ALFALFA Team 2008). ECO+A accounts for roughly 30% of the whole ECO sample (Moffett et al., submitted). Although ALFALFA is flux-limited, the combination of its flux limit and the ECO completeness limit is such that we can reliably determine whether a galaxy is gas-dominated \((M_{HI}/M_\star > 1)\) or not (see Moffett et al., submitted). Fig. 1 shows an on sky distribution of ECO galaxies with ECO+A galaxies boxed in magenta.

2.2. The Mock Catalog

The mock catalog used comes from an N-body dark matter simulation created by Andreas Berlind at Vanderbilt University and is designed to mimic the redshift coverage and magnitude limits of RESOLVE. The simu-
exploring the dependence of galaxy properties on group halo environment in the ECO catalog

Figure 1. On-sky distribution of ECO catalog galaxies. Each galaxy is color coded based on its group’s halo mass. Purple shaded regions cover ECO+A, and the RESOLVE A-semester is enclosed by the green dashed box.

In the simulation, dark matter halos are first identified using a Friends of Friends (FoF) halo-finding algorithm that uses a single linking length that is 0.2 times the average distance between particles (Davis & Dorygowski 1985). Note that halo finding in the mock is not subject to peculiar velocities since group finding is performed in real space. Also, because a FoF algorithm is used, the geometric shapes of identified dark matter halos are not restricted. Total halo masses are therefore known by summing the mass of the dark matter particles within each identified halo. All dark matter halos with mass greater than $M_{\text{min}}$ are given a central galaxy. These halos are then populated with a number of satellite galaxies that are assigned the velocity and spatial position of randomly selected dark matter particles within the identified halo. The parameters for choosing how many satellite galaxies each halo contains and $M_{\text{min}}$ are tuned such that the galaxy-galaxy correlation function and the total number density match what is observed. Each galaxy is also assigned a luminosity based on the conditional luminosity function (CLF) described in Cacciato et al. (2009), which gives the average number of galaxies in velocity space. Therefore longer values of $b_\perp$ are necessary since galaxy peculiar velocities in group environments drastically increase the separation between galaxies in velocity space. Therefore longer values of $b_\perp$ are necessary to link galaxies that reside in the same halo.

The method starts with a galaxy and links it to all friends of its galaxy, and so on until no more galaxies can be linked. To identify groups in both simulated and real catalogs, we again use a Friends of Friends (FoF) algorithm. This algorithm is similar to the method used for identifying dark matter halos in the mock with the difference of using two different linking lengths. One linking length links based on differences in line-of-sight velocity ($b_z$) while the other links galaxies according to their projected radial separate ($b_\perp$). Two distinct linking lengths are necessary since galaxy peculiar velocities in group environments drastically increase the separation between galaxies in velocity space. Therefore longer values of $b_\perp$ are necessary to link galaxies that reside in the same halo.

3. METHODS

Group finding, dynamical and HAM mass estimation, and virialization metrics are discussed here in detail.

3.1. Friends of Friends Algorithm

To identify groups in both simulated and real catalogs, we again use a Friends of Friends (FoF) algorithm. This algorithm is similar to the method used for identifying dark matter halos in the mock with the difference of using two different linking lengths. One linking length links based on differences in line-of-sight velocity ($b_z$) while the other links galaxies according to their projected radial separate ($b_\perp$). Two distinct linking lengths are necessary since galaxy peculiar velocities in group environments drastically increase the separation between galaxies in velocity space. Therefore longer values of $b_\perp$ are necessary to link galaxies that reside in the same halo.

The method starts with a galaxy and links it to all galaxies within a certain radius, which become the starting galaxy’s “friends”. All friends of linked galaxies become friends with the initial galaxy, and so on until no more galaxies can be linked (Li & Yee 2008; Huchra &
The two separate linking lengths are given in terms of the number density of the sample. The volume of the sample is therefore used to scale these lengths in terms of the mean distance between galaxies. The FoF algorithm is desirable because it will quickly produce a unique, deterministic solution for each set of chosen linking lengths, and does not impose a specific shape on the resulting groups.

The FoF algorithm faces several challenges when attempting to recover the true groupings. Because radial velocities can be strongly affected by the peculiar motions of galaxies, linking groups in velocity space can be particularly difficult. As a result, interloping galaxies will often appear and can sometimes act as a bridge, merging two isolated groups. Alternatively, group fragmentation can occur where group members are left out. In order to estimate how well FoF recovers certain group properties, Berlind et al. (2006) tested a grid of linking lengths and determined how varying the values of $b_1$ and $b_2$ will affect how well various group properties are recovered (see their Figure 3). These properties include velocity dispersion, projected group size, multiplicity function (the spatial density of groups as a function of their richness in members), and halo and group richness. No two values of the linking lengths will optimally recover all desired properties of the resulting groups. Berlind et al. (2006) chose $b_1 = 0.14$ and $b_2 = 0.75$, which optimally recovers group richness, projected group sizes, and the halo multiplicity function. However these linking lengths do not perform well at recovering group velocity dispersion. In §4.1 new linking lengths are proposed to better recover velocity dispersion in order to obtain more accurate dynamical masses.

### 3.2. Group Mass Measurements

We determine dynamical masses and HAM masses for FoF identified groups in the mock and ECO catalogs. Dynamical masses are also found for the true mock catalog groups.

Equation 1 was first applied to mock catalog groups in order to determine the best measure of $\sigma_z$ and virial radius, $r_{\text{vir}}$. Various definitions of these measurements were applied to true mock catalog groups whose resulting dynamical mass was then compared to their true halo mass. We found defining $\sigma_z$ as the standard deviation of the group’s velocity distribution from the average instead of the central galaxy produces a tighter relationship between dynamical mass and true halo mass. This is described by Eq. 2.

$$\sigma_z = \sqrt{\frac{\sum_i^N (c_i - \bar{c}_{\text{grp}})^2}{N - 1}}$$

To achieve the same goal of reducing the dispersion in determined mass, projected group radius was found by finding each group’s spatial center by averaging RA and DEC coordinates to get $\bar{\text{RA}}$ and $\bar{\text{DEC}}$. Each group member’s angular distance $\delta$ from these center coordinates was determined. The group radius, $R_{\text{avg}}$, is then determined by averaging the distances converted to Mpc as described by Eq. 3.

$$R_{\text{avg}} = \frac{\sum_i^N \delta_i \bar{c}_{\text{grp}}/H_0}{N}$$

Because $R_{\text{avg}}$ is not the same as $r_{\text{vir}}$, which is an input to Eq. 1, we use the mock catalog to find a relationship between the two. Assuming $r_{\text{vir}} = f * R_{\text{avg}}$ we can rewrite Eq. 1 as:

$$M_{\text{dyn}} = \frac{3\pi \sigma_z^2 (f * R_{\text{avg}})}{2} G$$

By plotting $\log M_{\text{halo}}$ against $\log M_{\text{dyn}}$ and fitting a line of slope 1, we can solve for the y-intercept of the best fit line, which translates to the log-multiplicative factor, $log(f)$, such that on average $M_{\text{halo}} = f * M_{\text{dyn}}$. Using different linking lengths slightly changes this factor $f$, but not significantly from $f = 1.27$ found using $M_{\text{dyn}}$ determined for the true mock catalog groups (i.e. pre-group finding). To determine dynamical masses for ECO groups we use the same methods described here and adopt $f = 1.27$ to convert $R_{\text{avg}}$ to $r_{\text{vir}}$.

We also find HAM masses for FoF identified groups following the abundance matching method described in Blanton & Berlind (2007). This method assumes a monotonic relationship between group luminosity and group mass, described by two functions. The first is a group cumulative luminosity function, $n(L)$, that comes from group catalogs. The second is a cumulative halo mass function, $n(M)$ that comes from a combination of concordance $\Lambda$CDM cosmology theory (Press & Schechter 1974) and N-body cosmological dark matter simulations. Specifically, $n(M)$ used for abundance matching in this paper came from the work done by Warren et al. (2006) who modified the shape of the theoretical halo mass function by fitting parameters to a series of N-body dark matter simulations. These HAM masses mainly differ from the dynamical masses in that they do not rely on the underlying observed group dynamics.

It is also important to recognize the different ways of defining theoretical mass. In the mock catalog being used for this study, halo mass is defined by summing the masses of dark matter particles grouped with a FoF algorithm, instead of being defined as $M_{200}^\text{vir}$, the mass enclosed within the surface where the enclosed density exceeds the average density of matter in the universe by a factor of 200. We must define the dynamical mass consistently to avoid producing an offset with HAM masses. It is for this reason we calibrate our calculations of $r_{\text{vir}}$ on the mock catalog as opposed to calibrating to $r_{200}$, which would produce dynamical masses defined as $M_{200}$. HAM masses are assigned using a theoretical halo mass function modified by fitting to simulations that use a FoF algorithm to identify halos as opposed to enforcing halo masses to be defined as $M_{200}$. Without this consistency we would encounter an offset in the comparison of HAM and dynamical masses.

Fig. 2 gives a simple comparison of the mass methods by showing the distribution of mock and ECO catalog group masses found using the two different methods. Fig. 2a shows the whole distribution of ‘true’ halo masses...
for mock catalog groups in addition to HAM masses of FoF extracted groups in both mock and ECO catalogs. More high mass clusters exist in the mock than is apparently recovered by the combination of group finding and assigning masses according to abundance matching. Fig. 2b shows a similar comparison with dynamical mass estimates and is limited to groups with \( N_{\text{grp}} \geq 5 \) in addition to the blue histogram that shows HAM masses for ECO groups with \( N_{\text{grp}} \geq 5 \). The distributions of dynamical masses of mock and ECO catalog groups post group finding are similar, and neither differs greatly from ECO HAM masses at \( M_{\text{halo}} > 12.5 \log M_\odot \). Differences do exist at masses lower than \( 12.5 \log M_\odot \) and at all masses these distributions differ from the distribution of dynamical masses of true mock catalog groups. See §4.2 for a more extensive breakdown of the differences between HAM and dynamical mass measurements performed before and after group finding.

3.3. Virial Radius & Virialization Metrics

Here we describe the methods for virialization measurements performed on observed groups.

3.3.1. The Anderson-Darling Test

To test whether a group is virialized or not, we follow Hou et al. (2009) in applying the Anderson-Darling (A-D) test to measure how similar each group's velocity distribution is to a Gaussian distribution. The A-D test requires the computation of two parameters, \( A^2 \) and \( A^{2*} \), which are given in equations 5 and 6. Here, \( Y_i \) for each group would be the set of velocities for galaxies in a group ordered from smallest to largest and \( \Phi(Y_i) \) is the CDF of a normal distribution for our case.

\[
A^2 = -n - \frac{1}{n} \sum_{i=1}^{n} \left(2i-1\right) \left(\ln \Phi(Y_i) + \ln \left(1 - \Phi(Y_{n+1-i})\right)\right) \tag{5}
\]

\[
A^{2*} = A^2 \left(1 + \frac{0.75}{n} + \frac{2.25}{n^2}\right) \tag{6}
\]

The parameter \( A^{2*} \) is an adjusted statistic used when both the mean and variance of the original distribution are unknown and can only be estimated from the \( Y_i \) values (D’Agostino 1986). Hou et al. (2009) use Monte Carlo simulations to conclude that the A-D test is reliable for groups with as low as 5 members. In order to understand the value \( A^{2*} \), the value \( \alpha \) is computed using Eq. 7 and represents the likelihood that the data comes from an underlying Gaussian distribution. We represent \( \alpha \) as a fractional probability, however it can exceed unity.

\[
\alpha = a e^{A^{2*}/b} \tag{7}
\]

The values a and b are found from Monte Carlo simulations to be 3.6789468 and 0.1749916, respectively (Hou et al. 2009; Nelson 1998). We determine the parameter \( \alpha \) for each group with \( N > 5 \) members, the minimum group size for which this test is reliable. Groups are considered not virialized if \( \alpha < 5\% \) (Hou et al. 2009).

3.3.2. Substructure

We strive to further characterize groups by measuring the degree of substructure within groups. In order to quantify the degree of substructure within a group we apply the Dressler-Schechtman (DS) test (Cohen et al. 2014). This test detects local variations in velocity dispersion, \( \sigma_{\text{loc}} \), and mean velocity, \( \bar{v}_{\text{loc}} \), around each galaxy by finding each galaxy’s 10 nearest neighbors and comparing their velocity distribution to that of the entire group. This is designed to detect differences between a galaxy’s local velocity mean and dispersion compared to \( \sigma \) and \( \bar{v} \) of the entire group (Dressler & Schechtman 1988).

The discrepancy for each galaxy is described by the parameter \( \delta \) given in Eq. 8.

\[
\delta^2 = {11/\sigma^2} [\left(\bar{v}_{\text{loc}} - \bar{v}\right)^2 + \left(\sigma_{\text{loc}} - \sigma\right)^2] \tag{8}
\]

The coefficient of 11 was decided upon by Dressler & Schechtman (1988) and sets the minimum group size to be 11 for performing this test. Taking the sum over \( \delta \) for all group members gives the cumulative deviation \( \Delta \). The value \( \Delta \) must be compared to \( \Delta_{\text{sim}} \), which is obtained by erasing any potential correlations between position and velocity within a group by scrambling the velocities assigned to each position coordinate. \( \Delta_{\text{sim}} \) is found just like \( \Delta \) for 1000 random reassignments of velocity. The probability, \( p \), that one of these \( \Delta_{\text{sim}} \) values is greater than the observed group \( \Delta \) is computed by taking \( p = N(\Delta_{\text{sim}} > \Delta_{\text{obs}})/N_{\text{sim}} \), where \( N_{\text{sim}} = 1000 \) (Cohen et al. 2014). Higher \( p \) values indicates a low likelihood for subclustering, while low \( p \) values suggest high subclustering within a group. The D-S test is applied to groups in ECO that have 11 or more members in order to classify groups with substructure.

4. RESULTS

Two types of results are presented below. Results pertinent to the methods for group finding and mass determination are given in §4.1 - 4.2. We present the uncertainties involved with determining dynamical mass and offer suggestions for future improvements by modifying
the group finding algorithm and identifying unvirialized systems in §4.3. Then in §4.4 we change focus, using our optimized halo mass and virialization metrics to study the environmental effects on various galaxy properties in the ECO catalog.

4.1. Optimization of Linking Lengths

In order to choose the best linking lengths for our purposes, dynamical masses have been calculated for mock catalog groups that were identified using a variety of possible linking lengths. Differences among these halo masses are solely due to changes in group memberships. Often, an increase in a galaxy’s group dynamical mass is due to more members being included in the group, which will increase the group velocity dispersion and/or average radius. For each set of linking lengths, we compare post-FoF dynamical masses, velocity dispersions, and average projected radii to those of the “true” groups on a galaxy by galaxy basis. We seek the linking lengths that produce the closest 1:1 relationship in these comparisons with the minimum scatter. Figure 3 shows this comparison for linking lengths of $b_\perp = 0.12$, $b_z = 1.3$ and $b_\perp = 0.14$, $b_z = 0.75$, respectively. This comparison shows the overall improvement in dynamical masses between the old linking lengths chosen by Berlind et al. (2006) and the values we choose. Increasing $b_\perp$ improves the dynamical masses by better recovering group velocity dispersions, as indicated by a comparison of Figures 3(b) and 3(e). This improvement keeps a majority of the galaxies centered along the one-to-one line. Increasing $b_z$ also reduces fragmentation, which is evidenced by the asymmetric scatter around the 1:1 line in Fig. 3(a) in comparison to Fig. 3(d). The former has a decreased number of groups with underestimated dynamical masses (those falling above the 1:1 line) due to an increase in $b_z$. This decrease in fragmentation for larger $b_z$ is desirable because little can be done to reconcile this mistake and these groups’ masses will be significantly underestimated. The problem of group merging remains fairly similar between the two linking lengths; however, it worsens for values of $b_z$ greater than 1.3 as shown. Because merging remains similar between linking lengths, but fragmentation is greatly reduced, we favor the linking lengths of $b_\perp = 0.12$ and $b_z = 1.3$. In addition we measure the correlation coefficient $\rho$ with the Spearman rank test for mass, velocity, and radius and find for all these parameters that linking lengths of $b_\perp = 0.12$ and $b_z = 1.3$ are slightly more correlated. The results for $\rho$ values are given in the corresponding frames in Fig. 3. A measure of the dispersion is also given in the same figure as $S$ and is found by summing the absolute value of the difference in $x$ and $y$ values and normalizing by the number of points. This test also shows less dispersion in the relationship between group mass and velocity before and after group finding when $b_\perp = 0.12$ and $b_z = 1.3$. The recovery of group radii is the least correlated in both cases and by eye one can tell from Fig. 3 (c) & (f) that group radii are on average much larger after group finding. The mistaken inclusion of originally isolated or unassociated galaxies lying in the outskirts of their new groups is a likely cause for the common increase in group average radius. Other linking lengths have been tested, and while increasing $b_z$ further does continue to improve group velocity dispersion accuracy, this change introduces more group merging and interlopers and therefore more scatter in the estimated dynamical masses. Therefore, linking lengths of $b_\perp =
0.12, $b_z = 1.3$ are determined to be the most appropriate linking lengths for determining dynamical masses.

In comparison Duarte & Mamon (2014) find that linking lengths of $b_{\perp} = 0.11$ and $b_z = 1.3$ recover 95% of galaxies within $r_{200}$ and 95% along the line of sight velocity, respectively. For environmental studies however, they suggest $b_{\perp} = 0.07$ and $b_z = 1.1$. In this case they acknowledge that shorter linking lengths will cause more fragmentation, especially in samples that are less complete. This increase in fragmentation is because the more galaxies that are missing, the more likely it is that there will be missing ‘links’ to other group members, especially for shorter linking lengths. Their study is different from our own in that their mock catalog has a different completeness level and higher redshift range, such that peculiar velocities are not such a large fraction of the redshift of a galaxy. Because our mock is designed to resemble the redshift limits and magnitude completeness levels of ECO, we trust our chosen linking lengths of $b_{\perp} = 0.12$, $b_z = 1.3$ and use them throughout this paper for mass estimates, unless otherwise noted.

While the linking lengths chosen on average improve the dynamical masses determined, there is still room for improvement. Fig. 3 shows values of $b_{\perp} = 0.12$ and $b_z = 1.3$ decrease group fragmentation and slightly increase the amount of mergers indicated by fewer extracted groups with underestimated masses and more with overestimated masses. Merging will often cause a negligible increase in the masses of larger groups (N > 10) since the addition of a handful of galaxies will not significantly alter the dynamical mass. This result can be inferred from Fig. 4 where the dynamical masses of galaxies in originally large, high mass groups remain in a 1:1 relationship with their original halo masses. By studying environmental effects on galaxies inside and outside the virial radius separately, we can eliminate galaxies that are not in equilibrium with the core of the group. In future studies, we suggest modifying the FoF algorithm by possibly having adaptive linking lengths, or by adding a second step to remove obvious non-members such as in Tempel et al. (2014). This modification however would remain distinct from spherical overdensity algorithms that impose a shape on extracted groups (Lacey & Cole 1994).

4.2. Comparison of Mass Measurements

It is of interest to compare the dynamical masses to the HAM masses found for galaxy groups in the mock and in ECO catalogs. Because the HAM masses do not directly depend on the virialization state of the group, we would expect substantial scatter in the agreement between the two methods. We apply the methods described in §3.2 to both the mock catalog true groups and mock catalog FoF extracted groups. We compare all these mass measurements to original halo masses in Fig. 4. Here, all comparisons show only groups with $N_{\text{grp}} \geq 3$. Fig. 4a compares the dynamical masses of true groups to their true halo mass and shows a systematic underestimation in dynamical mass that increases in effect for groups with fewer members. To avoid this effect we restrict our later analysis that uses these estimations of $M_{\text{dyn}}$ for ECO to groups with $N_{\text{grp}} \geq 5$. Panel b in Fig. 4 shows a similar comparison of true group HAM masses with their mock halo mass. This figure utilizes the entire simulation box. The scatter in this relationship comes from the random-ness in the assignment of galaxy luminosities to groups based on their halo mass when defining the mock catalog (§2.2). We believe the tapering of the scatter for groups with $M_{\text{halo}} < 12.0$ is due to the fact that random scatter was not added when populating halos with central galaxies, only satellites. The majority of these lower mass halos are isolated and contain only a central galaxy, so there is little luminosity scatter from populating these halos with satellite galaxies.

In addition to the scatter in Fig. 4b there is also a possible offset due to cosmic variance. The magnitude of this offset can be found using the results of Hu & Kravtsov (2003) who quantify the uncertainties due to cosmic variance and sample variance on perceived local cluster abundances (displayed in their Fig. 2). The relationship Hu & Kravtsov (2003) find can be scaled by $R_{\text{ECO}} = 37$ Mpc/h and $h = 0.7$ in order to find the possible shift in the halo mass function that would affect the ECO sample and represent this shift by the black arrow in the bottom left corner of Fig. 4d. This shift in the halo mass function would translate to shifts in HAM masses. In Fig. 4b we see very little shift from the one-to-one line indicating the effects of cosmic variance are not significant for the mock catalog. Nevertheless, this shift could still be present in the ECO sample depending on the extent to which cosmic variance affects it.

In comparing galaxies’ halo masses with their dynamical masses or HAM masses determined for FoF extracted groups (Fig. 4c,d), we can see the effects of the group finder. There is a population of galaxies in Fig. 4c,d that have high dynamical masses, but low halo masses. These galaxies were originally isolated or living in very low mass halos but were linked to larger groups and therefore inherited the larger halo mass. While a large number of these truly isolated galaxies are in the outskirts of their new groups, it is impossible to remove them using observable parameters without also removing true group members. It will therefore be just as unclear in the real data to discern whether an object is a true group member or not. The D-S test can be used to identify subgroups that were a possible result of the group finder merging two groups, however this test will be unable to identify spatially scattered field galaxies on the edges of a group. Fortunately, these misgrouped field galaxies do not significantly affect the dynamical or HAM masses of the original group, since the groups that were originally in high mass halos remain very close to the 1:1 line after group finding despite contamination from interlopers.

Despite the tighter trend in HAM masses pre-group finding, it is important to remember that there are uncertainties in the mass function used to assign HAM masses due to the effects of cosmic variance and differences in true group abundances compared to what is accepted. Additionally, these masses rely almost solely on luminosity, which relates to many of the group properties we later study in this paper. Therefore, in order to avoid introducing covariance between galaxy properties and estimated group masses we use the dynamical masses in the analysis of ECO groups and their galaxy member properties.

Fig. 5 plots HAM masses versus the corresponding dynamical masses galaxy by galaxy for (a) identified groups in ECO and (b) mock catalog post-FoF groups. In both figures HAM masses are slightly larger than dy-
Figure 4. Mass comparisons for the mock catalog. (a) Original halo masses plotted against dynamical masses of true groups. (b) Original halo masses plotted against HAM masses of true groups and reflects the random scatter in group luminosities assigned at fixed mock halo mass. The black arrow in the bottom left shows the possible shift due to cosmic variance in the halo mass function described in §4.2. Note: this plot uses data from the entire simulation box. (c) Dynamical masses of FoF extracted groups compared to their original halo masses. (d) HAM masses of FoF-extracted groups compared to original halo masses. The black arrow indicates the same possible offset due to cosmic variance as described for panel b. Each point is a galaxy, however if groups remain in their true halo after group finding then all galaxies in that group will be over-plotted on top of each other. Therefore, the scatter in the plot as an indication in the error on a single galaxy’s mass estimation is misleading because the density of points is not visualized. For all panels, only groups with FoF extracted group number \( N_{\text{gal}} \geq 3 \) are plotted. The color scale represents the number of members in each galaxy’s original ‘true group’, where dark blue corresponds to galaxies that were originally isolated before group finding. One-to-one lines are plotted in each frame in green and dispersion bars are shown in red, where the center is the median of that bin. In frames c and d bins are restricted to \( M > 12 \) in both the x and y axis to exclude the large population of dark blue outliers.

We additionally present the relationship between group mass and group size. Fig. 6 shows that this relationship follows a logarithmic trend in group number, with more scatter at low \( N_{\text{grp}} \). The color scale of Fig. 6 shows that HAM masses also produce the same trend. Groups with \( N_{\text{grp}} > 20 \) correspond to halos of mass approximately greater than \( 10^{13.5} M_\odot \).

### 4.3. Identifying Substructure

In order to gain more insight on group membership issues affecting group mass estimations, we apply the the Dressler-Schechtman (DS) test described in §3.3.2 to galaxy groups in ECO with the goal of identifying subgroup components. We also compare the results of this test with the Gaussianity of each group’s velocity distribution characterized by the Anderson-Darling test described in §3.3.1.

Values of \( \delta \) are found for each member galaxy of the groups with \( N \geq 11 \). Each group’s \( p \)-value is also found, which indicates the likelihood that the group contains substructure. Low \( p \)-values indicate higher likelihood of the presence of substructure. Groups with \( p \)-value \(< 0.01 \) are selected and the \( \delta \) parameter is used to select possible subgroups. In Fig. 7 three examples of groups with \( p-
values indicating the presence of substructure are shown. One group considered virialized as classified by both the A-D and D-S tests is also presented. Each galaxy is color coded by its $\delta$ value, which indicates how much the local velocity distribution deviates from the whole. Galaxies with similar $\delta$ values are not necessarily related, however regions of nearby galaxies that all contain similar $\delta$ values are. For the top three groups shown in Fig. 7 possible subgroups are selected based on their $\delta$ values (left panels) and the corresponding histograms of their velocity distributions are plotted (right panels). The redder points indicate the largest deviations, while the bluer points show the smallest. Likewise, the red histograms that show the high $\delta$ galaxies have a very narrow range in velocities, while the blue histograms for the low-$\delta$ galaxies cover a broader range of velocities, more closely resembling the overall velocity distribution for the groups (the purple histogram).

The groups shown in Fig. 7 are representative of the different types of interpretations that can be made based on velocity distributions. ECO group 4025 shows what could be a filament leading to a group. The filament (in blue) has a non-Gaussian velocity distribution, in contrast to the more circularly shaped group. ECO group 806 shows what could be two subgroups connected by a central structure. ECO group 5410 shows less obvious segregation in comparison to the first two groups, perhaps because the group has begun to relax and the subgroups components have begun mixing. These multiple-component groups will have overestimated dynamical masses due to larger measured radii and velocity dispersions. There are many cases where there are no obvious subgroups as seen in these examples. However, if subgroups were present and they were spatially overlapping and therefore appeared mixed, the D-S test would not be able to tell. In any case, this test serves as a powerful tool for identifying structures found by FoF that are not virialized or are really composed of multiple components. Using the D-S test to identify interesting systems that are not virialized will be the subject of future work.

In particular we would like to enhance this test by combining it with a center locating algorithm so subgroups can be systematically identified.

In Fig. 8 we compare the parameter $\alpha$ from the A-D test to the parameter $\delta$ from the D-S test. Each galaxy is defined a $\delta$ value, while only one $\alpha$ is assigned per group, resulting in a spread in $\delta$ for each $\alpha$ value, as seen in Fig. 8. A downward trend in the maximum galaxy $\delta$ value for increasing $\alpha$ is observed. This trend makes sense since low $\delta$ values indicate a low discrepancy in a galaxy’s local velocity distribution when compared to that of its group and high $\alpha$ indicates a Gaussian velocity distribution. Additionally, the color scale shows that $M_{dyn}$ correlates with both $\alpha$ and the highest galaxy $\delta$ value for a given group. To understand whether this correlation is due to a physical effect in galaxy groups or if it is related to the nature of the virialization tests we perform the same comparison to mock catalog groups before and after group finding (Fig. 8 middle & right panels). Mock catalog true groups do show the massive groups having higher maximum $\delta$ values with more spread, however the dependence on $\alpha$ is very weak. After group finding a similar trend in the mock catalog $\delta$ vs. $\alpha$ plot is observed with the groups with the highest mass groups having lower $\alpha$ and a larger spread in $\delta$. This suggests that the relationship between $\delta$, $\alpha$, and group mass for ECO groups is largely an effect of group finding. In this light, these tests prove useful for identifying when group finding went noticeably awry, and also for picking apart the subcomponents of large groups. More work is needed to improve these tests and also to consider the

![Figure 5. Comparison of dynamical masses to HAM masses for FoF extracted groups in ECO and mock catalogs. (a) Group halo mass methods compared for ECO groups with $3 \leq N_{grp} \leq 5$ shown in pink and those in groups with $N_{grp} > 5$ shown in Carolina blue. Groups with A-D classified non-Gaussian velocity dispersions ($\alpha < 5\%$) are depicted as navy stars. (b) A similar comparison for mock catalog FoF extracted groups. Larger triangular symbols represent groups with $N_{grp} > 5$ while smaller points represent groups with $3 \leq N_{grp} \leq 5$. The color scale matches that of Fig. 4.](image)

![Figure 6. Group number versus group dynamical mass is shown. Each group is also colored according to its group HAM mass. The horizontal purple line is showing the dividing line at $N_{grp} = 20$.](image)
Figure 7. Three groups that show evidence of dynamical substructure and one that does not. Scatter plots of each galaxy's coordinates are shown on top, color coded by the deviation, $\delta$, calculated for each galaxy according to Eq. 8. Symbol size is indicative of a galaxy's velocity relative to the group's mean velocity. We select similarly colored regions according their delta values and plot histograms of these region velocity distributions, colored to match the scatter plots to the left. The top purple histogram shows the velocity distributions for all group members. The fourth group is an example where no substructure was found. Its elongated shape exemplifies the fact that this test relies solely on velocity and not the spatial distribution of galaxies on the sky. ECO group 806 provides a good example of a system composed of multiple subgroups and an irregular shape. It is likely unvirialized with a larger total estimated mass due to the combination of these less massive subgroups.
4.4. Environmental Effect on Galaxy Properties

Color and star formation are studied in ECO groups in order to understand environmental effects on selected galaxy properties. We use our group dynamical mass estimates to characterize environment and also restrict our analysis to galaxies falling within the virial radius as define in §3.2, unless otherwise noted.

4.4.1. Color

To study environmental effects on galaxy color, we first study the distribution of galaxies on the blue and red sequences for systems of various sizes. The first analysis is displayed in Fig. 9, which shows the red and blue sequences (divided by $(u-r)^\alpha = 1.6$, see Moffett et al., submitted, for more accurate piece-wise division) in a plot of color versus stellar mass for ECO galaxies split into three subsets: field galaxies, groups with $3 < N_{grp} < 20$, and higher mass groups with $N_{grp} > 20$. It is clear that the fraction of blue sequence galaxies decreases significantly between field galaxies and galaxies living in high mass groups. We find that 80% of field galaxies ($N_{grp} = 1$) live on the blue sequence.

To study variations in galaxy color across group mass scales, the fraction of galaxies inside the virial radius that are on the red sequence of each ECO group is plotted against group dynamical mass in Fig. 10. There is a rough upward trend in the data indicating the presence of more red sequence galaxies dominating the population in higher mass halos. The transition to becoming red-sequence dominated appears to be gradual. However, for $M_{halo} > 13.5$ the red-sequence fraction remains uniformly above 40%, which is more clearly shown by the red histogram in Fig. 11. A KS test proves this distribution is very different than that of the blue histogram, which represents groups with $M_{halo} < 12.5$, with a probability of being drawn from the same sample of $5 \times 10^{-8}$. We can conclude there are a higher fraction of red-sequence galaxies in high mass halos and a higher fraction of blue-sequence galaxies in low mass halos. This result agrees with past studies such as that of Tanaka & Kodama (2004), who also find a higher fraction of red galaxies in group and cluster environments.

4.4.2. Gas Fraction

We also study the fraction of gas dominated galaxies as a function of halo mass for ECO+A groups (see §2.1). We defined gas dominated galaxies as having more HI mass than stellar mass and determine for each group the fraction of gas dominated galaxies within the virial radius. The results are shown in Fig. 12 where each group is color coded by its $\alpha$ parameter from the A-D virialization test. While there is a smaller subset of points because ECO+A is about a third the size of ECO, there is still a clear drop in the data past $M_{dyn} = 13.5 \log M_\odot$. After this mass scale groups uniformly contain fewer than 25% gas dominated galaxies within their virial radius, with the exception of one outlier, ECO group 806 presented in Fig. 7. This group is likely made of multiple components that are individually less massive than calculated dynamically for the whole group. If this is true, components of ECO group 806 would shift left on the plot and more closely follow the trend.

In Fig. 12 there are several groups that have no gas dominated galaxies within $r_{vir}$. These galaxies have $\alpha$ values lower than about 0.50, which is surprising because it is expected that lower gas content would associate with systems that are in a virialized state. However about 90% of these groups have 6 or fewer group members within their virial radii. The smaller number of group members makes the $\alpha$ measurement less robust and while the lack of gas dominated galaxies is significant, the small number of group members additionally makes it easier for the fraction to reach zero. No clear relation between $\alpha$ and fraction of gas dominated galaxies emerges, except for highly unvirialized ($\alpha < 0.05$) groups that tend to have a higher than average fraction of gas dominated galaxies. This trend supports the idea that unvirialized systems are less compact and less dense. Galaxies are still falling into these less dense systems and therefore these galaxies will be more capable of holding onto their gas.

4.4.3. Star Formation

To understand environmental effects on star formation activity, the median FSMGR (defined in §2.1) was found separately for galaxies inside and outside the virial radius in each group and plotted versus halo mass (Fig. 13). For these groups, the median FSMGR is on average higher in galaxies outside the virial radius than those within $r_{vir}$. This result is expected since processes such as ram pressure stripping and strangulation will occur first and more strongly for galaxies near the center of a group, where the density is higher than in the outskirts. It is interesting however, that past the mass scale of $10^{13.5} M_\odot$, the median FSMGR of galaxies both inside and outside the virial radius for all groups (except one outlier that is ECO Group 806 shown in Fig. 7), remains below 0.5. Even in this outlier group, median FSMGR within the virial radius still follows the trend, though as discussed in §4.3 and Fig. 7, this group’s mass is likely actually composed of the mass of three unvirialized subgroups. The reduction in scatter in median FSMGR past $10^{13.5} M_\odot$ suggests a physical change in all these groups causing a drastic, uniform decline in recent star formation. The mass scale of $10^{13.5} M_\odot$ has come up in other works including that of Robotham et al. (2006) who study galaxy luminosity functions (LF) for groups of varying group mass and find LF parameters stabilize starting at a mass of $10^{13.5} M_\odot$, suggesting that at this mass, processes such as quenching and merging are done occurring. This picture agrees with what is seen in Fig. 13, where a large fraction of groups below $10^{13.5} M_\odot$ have large FSMGR and therefore have had recent star formation activity, inside and outside $r_{vir}$, indicating that quenching processes have not yet suppressed all star formation.

Comparing to the results on color and HI in the previous sections, it is interesting to see these transitions in both the FSMGR, fraction of HI dominated galaxies, and the fraction of galaxies on the red sequence at the same mass scale. Additionally, we see changes in median FSMGR for galaxies outside the virial radius, meaning the influence of these dense group environments extends
past the virial radius. The extent of environmental effects past the virial radius has been seen in other studies including Bahé et al. (2013). Future work could involve determining the radius at which environmental effects are no longer seen.

5. Conclusion

We have determined a robust method for measuring dynamical masses of galaxy groups through optimization on a mock catalog. By comparing dynamical masses found for FoF extracted groups to those found for original mock catalog groups, we determined that FoF linking lengths of $b_2 = 0.12$ and $b_1 = 1.3$ reproduced the best group masses relative to other tested linking lengths.

Figure 8. Comparison of $\alpha$ and $\delta$ from the A-D and D-S tests, respectively. From left to right: ECO groups, mock catalog groups post-FoF, mock catalog true groups. Groups with $10 < N_{grp} < 25$ are shown in blue, groups with $25 \leq N_{grp} < 50$ are in red. Each point is a galaxy. High $\delta$ values indicate large discrepancies between a galaxy’s local velocity distribution and that of its groups. Large group $\alpha$ indicates a Gaussian velocity distribution and larger $\delta$ for a galaxy indicates a more discrepant local velocity distribution when compared to that of the whole group. Larger groups have lower $\alpha$ and a higher maximum $\delta$ value for both the ECO and post-FoF mock catalogs, but the true mock catalog shows the $\alpha$-dependence to be an artifact of group finding.

Figure 9. Extinction corrected color ($u - r$) versus stellar mass for field galaxies, galaxies in groups with fewer than 20 members, and galaxies in large groups with $N_{grp} > 20$. The relationship between halo mass and $N_{grp}$ is shown in Fig. 6. $N_{grp} = 20$ corresponds to roughly $10^{13.5} M_\odot$.

Figure 10. Fraction of galaxies inside $R_{vir}$ that are on the red sequence for ECO groups with $N_{grp} \geq 5$ plotted against group mass. Bars show the dispersion in the red sequence fraction and are positioned at the median for that bin. A vertical line is drawn at $M_{halo} = 13.5 \log M_\odot$ for reference. The fraction of galaxies on the red sequence for all isolated galaxies (not shown) is 20%.

Figure 11. Histograms showing the distribution of the fraction of galaxies on the red sequence in ECO groups, plotted in Fig. 10. The gray histogram shows the total for all groups and the colored histograms are defined by different ranges in halo mass. Groups with $M_{dyn} > 10^{13.5} M_\odot$ are uniformly composed of at least 40% red-sequence galaxies.

The improvement from prior linking lengths used by Berlind et al. (2006) was mostly a result of the improvement in estimated velocity dispersions for reconstructed groups, a parameter on which dynamical mass strongly depends. We also find that dynamical masses
by faults in the group finding where originally isolated galaxies are merged onto larger groups. However, these additional ‘merged’ galaxies do not significantly alter the mass of the original massive group.

The optimized dynamical mass methods were applied to the ECO catalog, which contains about 340 groups with $N_{grp} \geq 5$. We compared dynamical mass measurements of ECO groups to corresponding HAM masses and found a similar trend as in the same comparison performed using mock catalog groups. At high masses, HAM masses slightly exceed dynamical masses, whereas the trend switches for $M_{halo} < 12.5 \log M_\odot$. We find that in the mock catalog there are many galaxies that were originally isolated but were grouped onto larger groups and adopted the larger halo mass. This is presumably happening in ECO groups and therefore to reduce this effect when studying galaxy properties we split up groups into two subsets composed of group members residing either inside or outside the virial radius of their group. We believe using a modified FoF group finding algorithm could help with contamination from merged groups or unassociated edge galaxies, however this task is difficult. Because unvirialized groups would result in larger dynamical masses than expected for relaxed systems we use virialization tests to try to identify cases of unvirialization.

To assess the virialization state of ECO groups, two statistical methods, the A-D and D-S tests, were used that perform measures of group velocity distribution. The A-D test measures how Gaussian a group's velocity distribution is, while the D-S test returns a $p$-value that indicates how likely it is that a system contains substructure components. We find that when a group’s $p$-value indicates a high likelihood for the presence of substructure, the $\alpha$ parameter given by the A-D test agrees and suggests a non-Gaussian velocity distribution. For the groups with obvious substructure, it is easy to separate the likely subgroups according to each galaxy’s $\delta$ value. However, a more robust method of identifying the members and spatial centers of these subgroups must still be developed. For groups whose virialization state is unclear, the two statistics did not always agree. The D-S test could only be used on groups with more than 10 members and most groups with substructure according to their $p$-value were also among the highest mass groups. This relation seems to arise partly due to the nature of the test, but also in part due to the group finder, which increases the amount of contamination from interlopers and causes these groups to appear less virialized. For smaller groups it is also more possible for a fraction of a galaxy’s ten nearest neighbors to not all be related, therefore making it more difficult to identify substructure around that galaxy. While the D-S test identified groups with interesting internal dynamics, different tests for deducing the virialization state of groups of all sizes are desired. More analysis of the A-D test that judges the Gaussianity of a group’s velocity dispersion is needed, in addition to incorporating tests that utilize the projected spatial positioning of group members.

With the masses found for ECO groups, we have studied environmental effects on galaxy properties. We studied color, gas content, and star formation as a function of group mass. This analysis revealed that blue galaxies make up 80% of field galaxies, and red galaxies make up
a larger fraction of more massive galaxy groups. There is also a transitional mass scale at $10^{13.5} \, M_\odot$ above which group median FSMGR remains below 0.5 for all groups, indicating quenching processes have fully suppressed star formation in these massive systems. In future work, we wish to study these group properties as a function of radius from the group center.

6. ACKNOWLEDGEMENTS

I would like to thank my very supportive and helpful advisor Sheila Kannappan, as well as my summer research advisor Andreas Berlind for the many discussions about and help with the theoretical aspects of this project. Also many thanks to Amanda Moffett for making the ECO catalog and for her continued help. We acknowledge NSF funding support to Vanderbilt under REU grant PHY-1263045 and to the RESOLVE survey at UNC Chapel Hill under AST-0955368.

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